

DHAKA UNIVERSITY
AFFILIATED COLLEGES

First Year Syllabus
Department of Mathematics

Four Year B S Honours Course
Effective from the Session: 2017–2018

Affiliated Colleges
Subject: Mathematics
Syllabus for Four Year B S Honours Course

Effective from the Session: 2013-2014

Year wise Courses and marks distribution

FIRST YEAR

| Subject Code | Title | Marks | Credits |
|--|--|--------------|----------------|
| MAT 101 | Fundamentals of Mathematics | 100 | 3 |
| MAT 102 | Calculus I | 100 | 3 |
| MAT 103 | Linear Algebra I | 100 | 3 |
| MAT 104 | Analytic and Vector Geometry | 100 | 3 |
| MAT 150 | Math Lab I | | 2 |
| COM 100 | History of the Emergence of Independent Bangladesh | 100 | 4 |
| Any Two of the following Minor Subjects : | | | |
| | Physics | 6 Credits | |
| | Chemistry | 6 Credits | |
| | Statistics | 6 Credits | |
| | Economics | 6 Credits | |

Detailed Syllabus

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|-----------------------|-----------------------------|-------------------|-------------------|------------------|
| Subject Code | MAT 101 | Marks: 100 | Credits: 3 | Hours: 45 |
| Subject Title: | Fundamentals of Mathematics | | | |

Elements of logic: Mathematical statements, Logical connectives, Conditional and bi-conditional statements, Truth tables and tautologies, Quantifiers, Logical implication and equivalence, Deductive reasoning.

Set Theory : Sets and subsets, Set operations, Cartesian product of two sets, Operations on family of sets, De Morgan's laws.

Relations and functions:. Relations. Order relation. Equivalence relations. Functions. Images and inverse images of sets. Injective, surjective, and bijective functions. Inverse functions.

Real Number System: Field and order properties, Natural numbers, Integers and rational numbers, Absolute value and their properties, Basic inequalities. (Including inequalities of means, powers; inequalities of Cauchy, Chebyshev, Weierstrass).

Complex Number System: Field of Complex numbers, De Moivre's theorem and its applications.

Theory of Equations: Relations between roots and coefficients, Symmetric functions of roots, Sum of the powers of roots, Synthetic division, Des Cartes rule of signs, Multiplicity of roots, Transformation of equation.

Elementary number theory: Divisibility. Fundamental theorem of arithmetic. Congruences (basic properties only).

Summation of series: Summation of algebraic and trigonometric series.

Evaluation: Incourse Assessment: 30 Marks. Final examination (Theory, 3 hours): 70 Marks.

Eight questions of equal value will be set, of which any **five** are to be answered.

References:

1. S. Lipschutz, **Set Theory, Schaum's Outline Series.**
2. S. Barnard & J. M. Child, **Higher Algebra.**
3. W.L. Ferrar, **Algebra.**
4. P.R. Halmos, **Naive Set Theory.**
5. H. S. Hall and S. R. Knight, **Higher Algebra.**

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|-----------------------|------------|-------------------|-------------------|------------------|
| Subject Code | MAT 102 | Marks: 100 | Credits: 3 | Hours: 45 |
| Subject Title: | Calculus I | | | |

Functions & their graphs : Polynomial and rational functions, logarithmic and exponential functions, trigonometric functions & their inverses, hyperbolic functions & their inverses, combinations of such functions.

Limit and continuity: Definitions and basic theorems on limit and continuity. Limit at infinity & infinite limits, Computation of limits. Indeterminate forms (L'Hospital's rule)

Differentiation: Tangent lines and rates of change. Definition of derivative. One-sided derivatives. Rules of differentiation (proofs and applications). Successive differentiation. Leibnitz's theorem (proof and application). Related rates. Linear approximations and differentials.

Applications of Differentiation: Rolle's theorem, Mean value theorem. Maximum and minimum values of functions and related problems. Concavity and points of inflection. Optimization

problems.

Integration: Antiderivatives and indefinite integrals. Techniques of integration. Definite integration using antiderivatives. Fundamental theorems of calculus (proofs and applications). Basic properties of integration. Integration by reduction.

Applications of Integration: Arc lengths. Plane areas. Surfaces of revolution. Volumes of solids of revolution. Volumes by cylindrical shells. Volumes by cross sections.

Graphing in polar coordinates: Tangents to polar curves. Arc length in polar coordinates. Areas in polar coordinates.

Improper integrals : Tests of convergence and their applications. Gamma and Beta functions.

Approximation and Series: Taylor polynomials and series. Convergence of series. Taylor's series. Taylor's theorem and remainders. Differentiation and integration of series. Validity of Taylor expansions and computations with series.

Evaluation: Incourse Assessment: 30 Marks. Final examination (Theory, 3 hours): 70 Marks.

Eight questions of equal value will be set, of which any **five** are to be answered.

References:

1. H. Anton, I. C. Bivens and S. Davis, **Calculus: Early Transcendentals**, Wiley.
2. E.W. Swokowski, **Calculus with Analytic Geometry**, Brooks/Cole.
3. G. B. Thomas and R. L. Finney, **Calculus and Analytic Geometry**, Addison Wesley.
4. J. Stewart, **Single Variable Calculus: Early Transcendentals**, Cengage Learning.
5. G. Strang, **Calculus**, Wellesley-Cambridge.
6. R. Larson, R. P. Hostetler, F. H. Edwards and D. E. Heyd, **Calculus with Analytic Geometry**, Houghton Mifflin College Div.

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|-----------------------|------------------|-------------------|-------------------|------------------|
| Subject Code | MAT 103 | Marks: 100 | Credits: 3 | Hours: 45 |
| Subject Title: | Linear Algebra I | | | |

Matrices and Determinants:

Notion of matrix. Types of matrices. Algebra of matrices. Determinant function. Properties of determinants. Minors, Cofactors, expansion and evaluation of determinants. Elementary row and column operations and row-reduced echelon matrices. Invertible matrices. Different types of matrices, Rank of matrices.

Vectors in \mathbb{R}^n and \mathbb{C}^n : Review of geometric vectors in \mathbb{R}^2 and \mathbb{R}^3 spaces. Vectors in \mathbb{R}^n and \mathbb{C}^n . Inner product. Norm and distance in \mathbb{R}^n and \mathbb{C}^n .

System of Linear Equations: System of linear equations (homogeneous and non-homogeneous) and their solutions. Application of matrices and determinants for solving system of linear equations. Applications of system of equations in real life problems.

Vector Spaces: Notion of groups and fields. Vector spaces. Subspaces. Linear combination of vectors. Linear dependence of vectors. Basis and dimension of vector spaces. Row and column space of a matrix. Rank of matrices. Solution spaces of systems of linear equations.

Linear Transformation: Linear transformations. Kernel and image of a linear transformation and their properties. Matrix representation of linear transformations. Change of bases.

Eigenvalues and Eigenvectors: Eigenvalues and Eigenvectors. Diagonalization. Cayley-Hamilton theorem and its application.

Evaluation: Incourse Assessment: 30 Marks. Final examination (Theory, 3 hours): 70 Marks.

Eight questions of equal value will be set, of which any **five** are to be answered.

Books Recommended :

1. Howard Anton & Chris Rorres – *Elementary Linear Algebra with Application*.
2. Seymour Lipschutz (Schaum's Outline Series)-*Linear Algebra*.
3. Md. Abdur Rahman- *Linear Algebra*.

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|-----------------------|-------------------------------------|-------------------|-------------------|------------------|
| Subject Code | MAT 104 | Marks: 100 | Credits: 3 | Hours: 45 |
| Subject Title: | Analytic and Vector Geometry | | | |

Two-dimensional Geometry: Transformation of coordinates, Pair of straight lines (homogeneous second degree equations, general second degree equations representing pair of straight lines, angle between pair of straight lines, bisectors of angle between pair of straight lines), General equations of second degree (reduction to standard forms, identifications, properties and tracing of conics).

Three-dimensional Geometry: Coordinates, Distance, Direction cosines and direction ratios, Planes (equation of plane, angle between two planes, distance of a point from a plane), Straight lines (equations of lines, relationship between planes and lines, shortest distance). Spheres. Conicoids (basic properties).

Vector Geometry: Vectors in plane and space. Algebra of vectors. Rectangular Components. Scalar and Vector products. Triple scalar product. Applications of vectors to geometry (vector equations of straight lines and planes, areas and volumes).

Evaluation: Incourse Assessment: 30 marks. Final examination (Theory, 3 hours): 70 Marks.

Eight questions of equal value will be set of which **five** are to be answered. (taking at least one from each group).

References:

1. A.F.M. Abdur Rahman & P.K. Bhattacharjee, **Analytic Geometry and Vector Analysis**.
2. Khosh Mohammad, **Analytic Geometry and Vector Analysis**.
3. J. A. Hummel, **Vector Geometry**.
4. H. Anton, I. C. Bivens and S. Davis, **Calculus: Early Transcendentals**, Wiley.
5. E.W. Swokowski, **Calculus with Analytic Geometry**, Brooks/Cole; Alternate.

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|-----------------------|-------------------|-------------------|-------------------|------------------|
| Subject Code | MAT 150 | Marks: 100 | Credits: 2 | Hours: 45 |
| Subject Title: | Math Lab 1 | | | |

Problem solving in concurrent courses (e.g; Algebra, Calculus, Linear Algebra and Geometry) using MATHEMATICA/MATLAB.

Lab Assignments: There shall be at least 5 lab assignments.

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| Evaluation: Internal Assessment (Laboratory works) | 40 marks |
| Final Examination (Lab, 3 hours) | 60 marks |

**Mathematics Minor Courses
for
Honours Students of Different Departments of 7 Colleges other than Mathematics**

The minor courses in Mathematics is open to Honours students of other departments in the faculty of science. Each students will pursue such courses as are required by her/his parent department

FIRST YEAR

| Subject Code | Title | Marks | Credits |
|---------------------|------------------------------|--------------|----------------|
| MAM 101 | Fundamentals of Mathematics | 100 | 2 |
| MAM 102 | Calculus I | 100 | 2 |
| MAM 103 | Analytic and Vector Geometry | 100 | 2 |
| MAM 104 | Linear Algebra | 100 | 2 |

Detailed Syllabi

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|-----------------------|------------------------------------|-------------------|-------------------|------------------|
| Subject Code | MAM 101 | Marks: 100 | Credits: 2 | Hours: 30 |
| Subject Title: | Fundamentals of Mathematics | | | |

1. Sets and subsets. Set operations. Family of Sets. De Morgan's laws. Relations and functions: Cartesian product of sets. Relations. Equivalence relations. Functions. Images and inverse images of sets. Injective, surjective, and bijective functions. Inverse functions.
2. The Real number system: Field and order properties. Natural numbers, integers and rational numbers. Absolute value. Basic inequalities. (including inequalities involving means, powers; inequalities of Cauchy, Chebyshev, Weierstrass).
3. The Complex number system: Geometrical representation Polar form. De Moivre's theorem and its applications. Elementary number theory: Divisibility. Fundamental theorem of arithmetic. Congruences (basic properties only).
4. Summation of finite series: Arithmetic-geometric series. Method of difference. Successive differences.
5. Theory of equations: Synthetic division. Number of roots of polynomial equations. Relations between roots and coefficients. Multiplicity of roots. Symmetric functions of roots. Transformation of equations.

Evaluation: Incourse Assessment: 30 Marks. Final examination (Theory, 2 ½ hours): 70 Marks
Eight questions of equal value will be set, of which any **five** are to be answered.

References

1. S. Lipschutz, Set Theory, Schaum's Outline Series.
2. S. Barnard & J. M. Child, Higher Algebra.
3. W.L. Ferrar, Algebra.
4. P.R. Halmos, Naive Set Theory.

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|-----------------------|------------|-------------------|-------------------|------------------|
| Subject Code | MAM 102 | Marks: 100 | Credits: 2 | Hours: 30 |
| Subject Title: | Calculus I | | | |

A. Differential Calculus

1. Functions and their graphs (polynomial and rational functions, logarithmic and exponential functions, trigonometric functions and their inverses, hyperbolic functions and their inverses, combination of such functions). Limits of Functions: definition. Basic limit theorems (without proofs).
2. Limit at infinity and infinite limits. Continuous functions. Properties Continuous functions on closed and boundary intervals (no proofs required).
3. Differentiation: Tangent lines and rates of change. Definition of derivative. One-sided derivatives. Rules of differentiation (with applications). Linear approximations and differentials. Successive differentiation. Leibnitz theorem. Rolle's theorem: Lagrange's mean value theorems. Extrema of functions, problems involving maxima and minima.

B. Integral Calculus

4. Integrals: Antiderivatives and indefinite integrals. Techniques of integration. Definite integration using antiderivatives.
5. Definite integral as a limit of a sum. The fundamental theorem of calculus. Integration by reduction.
6. Application of integration: Plane areas. Solids of revolution. Volumes by cylindrical shells. Volumes by cross-sections. Arc length and surface of revolution.

Evaluation: Incourse Assessment: 30 Marks. Final examination (Theory, 2 ½ hours): 70 Marks
Eight questions of equal value will be set, of which any **five** are to be answered.

References

1. H. Anton et al, Calculus with Analytic Geometry.
2. E.W. Swokowski, Calculus with Analytic Geometry.
3. L. Bers & P. Karal, Calculus.
4. S. Lang, A First Course in Calculus.

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|-----------------------|------------------------------|-------------------|-------------------|------------------|
| Subject Code | MAM 103 | Marks: 100 | Credits: 2 | Hours: 30 |
| Subject Title: | Analytic and Vector Geometry | | | |

Two-dimensional geometry

1. Coordinates in two dimension. Transformations of coordinates.
2. Reduction of second degree equations to standard forms. Pairs of straight lines. Identifications of conics. Equations of conics in polar coordinates.

Three-dimensional geometry

3. Coordinates in three dimensions. Direction cosines, and direction ratios.
4. Planes, straight lines and conicoids (basic definitions and properties only)

Vector geometry

5. Vectors in plane and space. Algebra of vectors. Scalar and vector products. Triple scalar products. Applications to Geometry.

Evaluation: Incourse Assessment: 30 Marks. Final examination (Theory, 2 ½ hours): 70 Marks
Eight questions of equal value will be set, of which any **five** are to be answered.

References

1. A.F.M. Abdur Rahman & P.K. Bhattacharjee, Analytic Geometry and Vector Analysis.
2. Khosh Mohammad, Analytic Geometry and Vector Analysis.
3. J. A. Hummel, Vector Geometry.

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|-----------------------|-----------------------|-------------------|-------------------|------------------|
| Subject Code | MAM 104 | Marks: 100 | Credits: 2 | Hours: 30 |
| Subject Title: | Linear Algebra | | | |

1. Matrices and Determinants:

Notion of matrix. Types of matrices. Matrix operations, laws of matrix Algebra. Determinant function. Properties of determinants. Minors, Cofactors, expansion and evaluation of determinants. Elementary row and column operations and row-reduced echelon matrices. Invertible matrices. Block matrices.

2. System of Linear Equations:

Linear equations. System of linear equations (homogeneous and non-homogeneous)and their solutions. Application of matrices and determinants for solving system of linear equations.

3. Vector Spaces:

Vectors in R^n and C^n :

Review of geometric vectors in R^2 and R^3 space. Vectors in R^n and C^n . Inner product. Norm and distance in R^n and C^n . Abstract vector space over R and C . Subspace. Sum and direct sum of sub spaces. Linear independence of vectors; basis and dimension of vector spaces. Row and column space of a matrix; rank of matrices. Solution spaces of systems of linear equation.

4. Linear transformations. Kernel and image of a linear transformation and their properties. Matrix representation of linear transformations. Change of bases.
5. Eigenvalues and eigenvectors. Diagonalization. Cayley Hamilton theorem. Applications.

Evaluation: Incourse Assessment: 30 Marks. Final examination (Theory, 2 ½ hours): 70 Marks
Eight questions of equal value will be set, of which any **five** are to be answered.

References

1. H. Anton, and C.Rorres, Linear Algebra with Applications, 7th Edition,
2. S. Lipshutz, Linear Algebra, Schaum's Outline Series.
3. W. Greub, Linear Algebra.

ECO 101: Principles of Microeconomics (3 credits)

1. Introduction: The economic way of thinking. Microeconomics and Macroeconomics. The basic problems of economic organization. Production and exchange- the Production-Possibility Frontier, the market mechanism.
2. Demand and consumer behaviour. Choice and utility theory. The Paradox of value. Law of diminishing marginal utility. Why the demand curve slopes downward. Consumer surplus. Normal inferior and Giffen goods. From individual to market demand. Basic elements of demand and supply. The demand curve; movement along the curve vs. shifts of the curve. The supply curve: movement along the curves. shift of the curve. Equilibrium with supply and demand curve.
3. Applications of demand and supply. Elasticity of demand and supply. Price, cross and income elasticity. The paradox of the bumper harvest. Impact of a tax/subsidy on price and quantity; price floors and ceilings the minimum wage controversy. Theory of production. The production function. Fixed factors vs. variable factors of production. Short-run and long-run. Total, average and marginal product. The law of diminishing returns. Returns to scale. Technological change.
4. Analysis of costs and profit. Fixed and variable costs. Total average and marginal costs. The link between production and costs. Marginal product and the least-cost rule. Opportunity costs. Accounting profit. economic profit. Profit-maximizing conditions. Perfect Competition: Profits, losses, break-even and shut-down condition. The firm's supply curve. Industry supply curve. Short-run and long-run equilibrium. Efficiency of perfect competition.
5. Monopoly: Sources of market imperfections. Monopoly equilibrium. Price discrimination. Natural monopoly and its regulation deadweight loss due to monopoly. Monopolistic competition and oligopoly; game theory. Market failures. Risk and uncertainty. Moral hazard and adverse selection.
6. Public goods and externalities. Coase theorem. The labour market. The demand for and supply of labour. Equilibrium in a competitive labour market Monopsony. Bilateral monopsony. The distribution of income and wealth. The Lorenz curve.
7. International trade: Comparative advantage and the gains from trade. Protectionism.

Textbook

1. Samuelson, P.A. and Nordhaus, W D., Economics
2. Lipsey, R., Positive Economics
3. Baunol, W. and Blinder, A., Economics: Principles and Policy

ECO 102: Principles of Macroeconomics (3 Credits)

1. Introduction to macroeconomics, Inflation, unemployment, the natural rate of unemployment, nominal and real GDP, business cycles, budget deficit and international deficit.
2. Measuring aggregate output and; the price level. Circular flow of income; injections and Leakages. Three alternative ways of measuring GDP. The accuracy in measured GDP. The CPI and the GDP deflator. Aggregate demand and aggregate supply. Short-run and long run aggregate supply. Shifts in aggregate demand and aggregate supply curves. Macroeconomic equilibrium.
3. Aggregate expenditure decisions. Private consumption, private investment, government purchases of goods and services, net exports. Autonomous and induced expenditure. Equilibrium expenditure and output. The autonomous expenditure multiplier. Relationship between the aggregate expenditure and aggregate demand curves; derivation of the aggregate demand curve.
4. Money and banking, Definitions and functions of money. The economic functions of financial intermediaries. How banks create money. The simple money multiplier. The central Bank and open market operations. The money multiplier. Interest rate determination. The demand for money. Interest rates and bond prices. Money market equilibrium.
5. Aggregate demand fluctuation. Monetary and fiscal policy transmission mechanisms. Time lags. Crowding out, international crowding out. Relative effectiveness of monetary and fiscal policy.
6. The labour market and aggregate supply. The flexible wage theory. The sticky wage theory. The long run and short-run aggregate supply curves.
7. Expectations and inflation. Anticipated and unanticipated inflation. Costs of inflating. Demand, pull and cost-push inflation. Adaptive expectations, rational expectations and their policy implications. The short-run and long-run phillips curves. Hysteresis Stabilising the economy: Macroeconomic policy targets and instruments. Conflicts between objectives. Fixed rules vs. feedback rules.

Textbook

1. Parking, M., Macroeconomics.
2. Samuelson, P.A. and Nordhaus, W.D. Economics.

DHAKA UNIVERSITY
AFFILIATED COLLEGES

Second Year Syllabus
Department of Mathematics

Four Year B S Honours Course
Effective from the Session: 2018–2019

Affiliated Colleges
Subject: Mathematics
Syllabus for Four Year B S Honours Course

Effective from the Session: 2018-2019

Year wise Courses and marks distribution

SECOND YEAR

| Subject Code | Title | Marks | Credits |
|--|------------------------------------|--------------|----------------|
| MAT 201 | Calculus II | 100 | 3 |
| MAT 202 | Ordinary Differential Equations I | 100 | 3 |
| MAT 203 | Numerical Analysis I | 100 | 3 |
| MAT 204 | Programming Fundamentals (Fortran) | 100 | 3 |
| MAT 250 | Math Lab II (Fortran) | 100 | 2 |
| MAT 299 | Viva Voce | 100 | 2 |
| Any Two of the following Minor Subjects : | | | |
| | Physics | 6 Credits | |
| | Chemistry | 6 Credits | |
| | Statistics | 6 Credits | |
| | Economics | 6 Credits | |

Detailed Syllabi

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|-----------------------|--------------------|-------------------|-------------------|------------------|
| Subject Code | MAT 201 | Marks: 100 | Credits: 3 | Hours: 45 |
| Subject Title: | Calculus II | | | |

A. Differential Calculus

1. Vector-valued functions of a single variable: Limits, derivatives and integrals of vector valued functions.
2. Tangent lines to graphs of vector-valued functions . Arc length from vector view point. Arc length parametrization.
3. Curvature of plane and space curves: Curvature from intrinsic equations, Cartesian equations and parametric equations. Radius of curvature. Centre of curvature,
4. Partial Differentiation: Functions of several variables. Graphs of functions of two variables. Limits and continuity. Partial derivatives. Differentiability, linearization and differentials. The Chain rule. Partial derivatives with constrained variables. Directional derivatives; gradient vectors and tangent planes.
5. Extrema of functions of several variables, Lagrange multipliers. Taylor's formula.

B. Integral Calculus

1. Multiple integrals: Double integrals and iterated integrals. Area as a double integral. Double integrals in polar form.
2. Triple integrals and iterated integrals. Volume as a triple integral. Triple integral in cylindrical and spherical polar coordinates.
3. General multiple integrals. Change of variables in multiple integrals. Jacobians.

Evaluation: Incourse Assessment 30 Marks. Final examination (Theory, 3 hours). 70 Marks
Eight questions of equal value will be set, of which any **five** are to be answered.

References

1. H. Anton et al, Calculus with Analytic Geometry.
2. E. Swokowski, Calculus with Analytic Geometry.
3. L. Bers & P. Karal, Calculus with Analytic Geometry.
4. S. Lang, Calculus of Several Variables.

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|-----------------------|--|-------------------|-------------------|------------------|
| Subject Code | MAT 202 | Marks: 100 | Credits: 3 | Hours: 45 |
| Subject Title: | Ordinary Differential Equations I | | | |

1. Ordinary differential equations and their solutions: Classification of differential equations. Solutions: Implicit solutions. Singular solutions. Initial value problems. Boundary value problems. Basic existence and uniqueness theorems (statement and illustration only). Direction fields. Phase line.
2. Solution of first order equations: Separable equations and equations reducible to this form. Linear equations, Exact equations, Special integrating factors, Substitutions and transformations,
3. Modelling with first order differential equations: Construction of differential equations as mathematical models (exponential growth and decay, heating and cooling, mixture of solutions, series circuit, logistic growth, chemical reaction, falling bodies). Model solutions and interpretation of results. Orthogonal and oblique trajectories.
4. Solution of higher order linear differential equations: Linear differential operators. Basic theory of linear differential equations. Solution space of homogeneous linear equations. Fundamental solutions of homogeneous systems. Reduction of order. Homogeneous linear equations with

constant coefficients. Nonhomogeneous equation. Method of undetermined coefficients. variation of parameters. Euler-Cauchy differential equations.

5. Modelling with second-order equations: Vibration of a mass on a spring, free and undamped motion; free and damped motion; forced motion; resonance phenomena; electric circuit problems, motion of a rocket.

Evaluation: Incourse Assessment 30 Marks. Final examination (Theory, 3 hours). 70 Marks

Eight questions of equal value will be set, of which any **five** are to be answered.

References

1. S. L. Ross, Differential Equation.
2. D. G. Zill, A First Course in Differential Equations with Applications.
3. F. Braner & J. A. Nohel, Differential Equations.
4. H.J.H. Piaggio, An Elementary Treatise on Differential Equations.

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|-----------------------|-----------------------------|-------------------|-------------------|------------------|
| Subject Code | MAT 203 | Marks: 100 | Credits: 3 | Hours: 45 |
| Subject Title: | Numerical Analysis I | | | |

1. Solution of equation in one variable: Bisection algorithm, Method of false position. Fixed point iteration, Newton-Raphson method, Error Analysis for iterative method, Accelerating limit of convergence.
2. Interpolation and polynomial approximation: Taylor polynomials, Interpolation and Lagrange polynomial, Iterated interpolation, Extrapolation.
3. Differentiation and Integration: Numerical differentiation, Richardson's extrapolation, Elements of Numerical Integration, Adaptive quadrature method, Romberg's integration, Gaussian quadrature.
4. Solutions of linear systems: Gaussian elimination and backward substitution, pivoting strategies, LU decomposition method.

Evaluation: Incourse Assessment 30 Marks. Final examination (Theory, 3 hours). 70 Marks

Eight questions of equal value will be set, of which any **five** are to be answered.

References :

1. R.L. Burden & J.D. Faires, Numerical Analysis.
2. M.A.Celia & W.G. Gray, Numerical Methods for Differential Equations.
3. L.W. Johson & R.D. Riess, Numerical Analysis.

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|-----------------------|---|-------------------|-------------------|------------------|
| Subject Code | MAT 204 | Marks: 100 | Credits: 3 | Hours: 45 |
| Subject Title: | Programming Fundamentals (FORTRAN) | | | |

1. Brief Introduction to Computer: Computer system, Information Processing Cycle, Operating System, Data representation in Computer
2. Program Design: Algorithm, Flowchart, Conditional Branching, Loop
3. Programming Language: Fortran and its History
4. Basic Elements of Fortran: Character set, Structure of Fortran statement, Program Structure, Data type, Constants, Variables, Operators and Operations, Intrinsic Functions, List directed I/O
5. Control Structures: Branches, Loops
6. Arrays: One dimensional array, Two dimensional array
7. Input/Output concept: Formatted I/O, File Handling
8. Subprogram: Subroutine, User defined function

- Implementation: Construction of Fortran program for problems drawn from mathematics and sciences including root finding problem for equation of one variable, IVP.

Classes: Theory (2 hours/week), Lab (At least 5 assignments).

Evaluation:

Internal Assessment (Lab / Incourse Examination) 30 Marks

Final examination (Theory, 3 hours) 70 Marks

References

- Introduction to Fortran 90/95 for Scientists and Engineers by Stephen J. Chapman.
- Modern Fortran Explained. Michael Metcalf, John Reid and Malcolm Cohen.
- Gordon B. Davis & Thomas R. Hoffmann, FORTRAN 77: A Structured, Disciplined Style.

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|-----------------------|-----------------------|-------------------|-------------------|------------------|
| Subject Code | MAT 250 | Marks: 100 | Credits: 2 | Hours: 45 |
| Subject Title: | Math Lab II (Fortran) | | | |

Problem solving in concurrent courses (e.g; Algebra, Calculus, Linear Algebra and Geometry) using MATHEMATICA/MATLAB.

Lab Assignments: There shall be at least 5 lab assignments.

Evaluation: Internal Assessment (Laboratory works) 40 marks

Final Examination (Lab, 3 hours) 60 marks

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|-----------------------|-----------|-------------------|-------------------|--|
| Subject Code | MAT 299 | Marks: 100 | Credits: 2 | |
| Subject Title: | Viva Voce | | | |

Viva Voce on courses taught in the First Year and Second Year

**Mathematics Minor Courses
for
Honours Students of Different Departments of 7 Colleges other than Mathematics**

The minor courses in Mathematics is open to Honours students of other departments in the faculty of science. Each students will pursue such courses as are required by her/his parent department

SECOND YEAR

| Subject Code | Title | Marks | Credits |
|--------------|---------------------------------|-------|---------|
| MAM 201 | Calculus II | 100 | 2 |
| MAM 202 | Ordinary Differential Equations | 100 | 2 |
| MAM 203 | Numerical Analysis | 100 | 2 |
| MAM 204 | Mathematical Methods | 100 | 2 |

Detailed Syllabi

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|-----------------------|--------------------|-------------------|-------------------|------------------|
| Subject Code | MAM 201 | Marks: 100 | Credits: 2 | Hours: 30 |
| Subject Title: | Calculus II | | | |

A. Differential Calculus

1. Vector-valued functions of a single variable: Limits, derivatives and integrals of vector valued functions. Tangent lines to graphs of vector-valued functions . Curvature of plane and space curves:
2. Partial Differentiation: Functions of several variables. Limits and continuity. Partial derivatives. Differentiability, linearization and differentials. The Chain rule. Partial derivatives with constrained variables. Directional derivatives; gradient vectors and tangent planes.
3. Taylor's formula (in one and in several variables). Extrema of functions of several variables, Lagrange multiplier.

B. Integral Calculus

4. Multiple integrals: Double and triple integrals; and iterated integrals. Area as a double integral. Double integrals in polar form. Volume as a triple integral. Triple integral in cylindrical and spherical polar coordinates.
5. General multiple integrals. Change of variables in multiple integrals. Jacobians.
6. Gradient, divergence, curl. Green's theorem, Gauss's theorem, Stoke's theorem.

Evaluation: Incourse Assessment 30 Marks. Final examination (Theory, 2 ½ hours). 70 Marks
Eight questions of equal value will be set, of which any **five** are to be answered.

References

4. H. Anton et al, Calculus with Analytic Geometry.
5. E. Swokowski, Calculus with Analytic Geometry.
6. L. Bers & P. Karal, Calculus with Analytic Geometry.

4. S. Lang, Calculus of Several Variables.

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|-----------------------|--|-------------------|-------------------|------------------|
| Subject Code | MAM 202 | Marks: 100 | Credits: 2 | Hours: 30 |
| Subject Title: | Ordinary Differential Equations | | | |

1. Ordinary differential equations and their solutions: Initial value problems. Boundary value problems. Basic existence and uniqueness theorems (statement and illustration only).
2. Solution of first order equations: Separable equations and equations reducible to this form. Linear equations, Exact equations, Special integrating factors, Substitutions and transformations,
3. Solution of higher order linear differential equations: Solution space of homogeneous linear equations. Fundamental solutions of homogeneous systems. Reduction of order. Homogeneous linear equations with constant coefficients. Nonhomogeneous equations.
4. Method of undetermined coefficients. variation of parameters. Euler-Cauchy differential equations.
5. Systems of differential equations, Linear system, Fundamental matrix. Solutions of linear systems, with constant coefficient.

Evaluation: Incourse Assessment 30 Marks. Final examination (Theory, 2 ½ hours). 70 Marks **Eight** questions of equal value will be set, of which any **five** are to be answered.

References

1. S. L. Ross, Differential Equation.
2. D. G. Zill, A First Course in Differential Equations with Applications.
3. F. Branner & J. A. Nohel, Differential Equations.
4. H.J.H. Piaggio, An Elementary Treatise on Differential Equations.

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|-----------------------|---------------------------|-------------------|-------------------|------------------|
| Subject Code | MAM 203 | Marks: 100 | Credits: 2 | Hours: 30 |
| Subject Title: | Numerical Analysis | | | |

1. Solution of equation in one variable: Bisection algorithm, Method of false position. Fixed point iteration, Newton-Raphson method, Error Analysis for iterative method, Acceleration of convergence.
2. Interpolation and polynomial approximation: Taylor polynomials, Interpolation and Lagrange polynomial, Iterated interpolation, Extrapolation.
3. Differentiation and Integration: Numerical differentiation, Richardson's extrapolation, Elements of Numerical Integration, Adaptive quadrature method, Romberg's integration, Gaussian quadrature.
4. Solutions of linear systems: Gaussian elimination and backward substitution, pivoting strategies, Matrix inversion; LU decomposition method.

Evaluation: Incourse Assessment 30 Marks. Final examination (Theory, 2 ½ hours). 70 Marks **Eight** questions of equal value will be set, of which any **five** are to be answered.

References :

1. R.L. Burden & J.D. Faires, Numerical Analysis.
2. M.A.Celia & W.G. Gray, Numerical Methods for Differential Equations.
3. L.W. Johnson & R.D. Riess, Numerical Analysis.

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| Subject Code | MAM 204 | Marks: 100 | Credits: 2 | Hours: 30 |
| Subject Title: | Mathematical Methods | | | |

1. **Fourier Series:** Fourier Series, Fourier sine and cosine series. Properties of Fourier series. Operations on Fourier series. Complex form.
2. Solution of differential equations in infinite series. Equations of Legendre, Bessel, Hermite and Laguerre. Special functions: Legendre, Hermite and Laguerre polynomials; Bessel functions. Generating functions and recurrence relations.
3. Beta and Gamma functions.
4. **Laplace transforms:** Basic definitions and properties, Existence theorem.. Laplace transforms of periodic functions. Transforms of convolutions. Inverse transform. Use of Laplace transforms in solving initial value problems.
5. Functions of a complex variable, analytic functions. Complex integration; Cauchy's theorem and Cauchy's integral formula. Singularities and residues. Cauchy's residue theorem. Evaluation of real integrals using contour integration.

Evaluation: In-course Assessment 30 Marks. Final examination (Theory, 2 ½ hours). 70 Marks
Eight questions of equal value will be set, of which any **five** are to be answered.

References

1. W.N. Lebedev & R.A. Silverman, Special Functions and their Applications.
2. E. Kreyszig, Advanced Engineering Mathematics.
3. M. R. Spiegel, Laplace Transforms, Schaum's Outline Series.
4. R.V. Churchill & J. W. Brown, Complex Variables and Applications.